

Course: B. Tech in Electrical Engineering **Sem:** IV

Subject Code: BTEEPE405B

Subject Name: Signals & System

Unit-1

(1) Find the energy and power of following Signal/Sequence

(i) $x[n] = 2^n u[-n]$

(ii) $x(t) = \text{Rect} \frac{t}{T}$

(iii) $\int_{-\infty}^{\infty} \{\delta(t)\cos 2t + \delta(t-2)\sin 2t\} dt$

(iv) $\int_{-0}^{2\pi} \{t \sin t \delta(\frac{\pi}{2} - t)\} dt$

(2) Sketch the following signals:

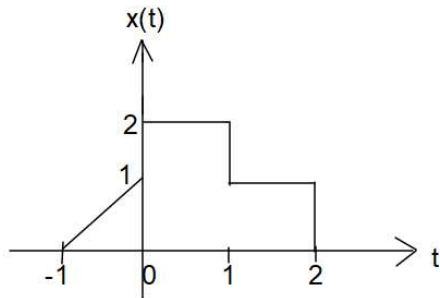
(i) $u[n+2] u[-n+3]$

(ii) $-2u(t+2)$

(iii) $\pi(t-2)$

(3) If $X[n] = \{1,2,3,4,1\}$, then: Find $x[2n-3]$ and plot $x[2n/3]$ and plot $x[-2n]$

(4) Plot $x(2t + 1)$ and $x(2 - 3t)$ from the following signal:



(5) Check for the periodicity of following signals and find the fundamental time period if they are periodic:

(i) $x[n] = e^{j2\pi n+2}$

(ii) $x(t) = 2 + \sin(2t) + \cos(3\pi t)$

(iii) $x(t) = 2u(t) + \sin^2(3\pi t)$

(iv) $x(n) = (\frac{1}{2})^n u[n]$

Unit-2

1. Define systems. Write the properties of the systems.
2. Check the following systems for Static/Dynamic/Causal/Non-Causal
(i) $y[n] = 2x[n + 1] + 3x[n] - x[n - 1]$ (ii) $y(t) = \frac{dx(t)}{dx} + x^2(t) + x(t + 1)$
3. Explain the process of checking linearity property of the system in detail.
4. Check whether the following systems are Stable/Unstable.
(i) $y(t) = t.x(t)$
(ii) $y(t) = u(t) + 2$
(iii) $y(t) = \sin(t).u(t)$
(iv) $y(t) = x(t)/t$
5. Describe the causal and non-causal systems

Unit-3

1. Define transfer function and write the properties of LTI system.
2. write the properties of convolution.
3. Find the convolution of following signals
(i) $x(t) = u(t)-u(t-2)$ and $y(t) = u(t)- u(t-1)$
(ii) $x(t) = \text{rect}(t/T)$ and $y(t) = \Delta(t/T)$
(iii) $x(t) = u(t+5)$ and $y(t) = \delta(t-7)$
(iv) $x(t) = u(t)$ and $y(t) = 2u(t+2)-3u(t+1)+u(t-2)$
4. How the causality and stability of the system can be checked by impulse response of the system explain in detail.

Unit-4

1. Find the Laplace transform of following signals and define ROC.
(i) $x(t) = u(t). e^{-(2t+1)}$
(ii) $x(t) = \sin 2t. e^{2t}. u(2t)$
(iii) $x(t) = u(t) - u(2t-1)$
(iv) $x(t) = [t^2 + 3t - 7]. u(t-1)$
(v) $x(t) = t. \sin t. u(t)$
2. Find the impulse response in time domain of the following systems, if systems are stable and causal.
(i) $H(S) = \ln \left(\frac{S+5}{S+6} \right)$
(ii) $H(S) = \frac{2S+5}{S^2+5S+6}$
(iii) $H(S) = 6S^2 + 1$

3. Consider a Continuous time LTI system for which input $x(t)$ and output $y(t)$ are related by the following differential equation

$$\frac{d^2y(t)}{dt^2} - \frac{dy(t)}{dt} - 2y(t) = x(t)$$

Determine $h(t)$

- (i) When system is Causal
- (ii) When the system is stable
- (iii) When the system is neither causal nor stable

4. Find Z- transform of following signals, and comment on ROC.

- (i) $x[n] = \{1, 2, 3\}$
- (ii) $x[n] = 3^n u[n] - 2^n u[-n-1]$
- (iii) $x[n] = \text{Sgn}[n]$
- (iv) $x[n] = 2^{|n|}$
- (v) $x[n] = (\frac{1}{2})^n u[-n-1]$

5. Consider a LTI system with following input output relationship:

$$Y[n] = (\frac{1}{2}) \cdot y[n-1] = x[n] - 2x[n-1]$$

Calculate:

- (i) system function.
- (ii) output $y[n]$ for input $x[n] = u[n]$

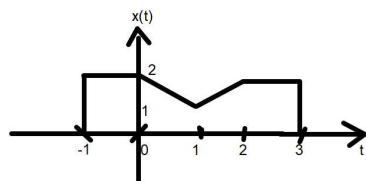
Unit-5

1. Derive the relation between Laplace transform and Fourier transform.

2. Find the Fourier transform of following signals and plot the magnitude and Fourier spectrum:

- (i) $x(t) = e^{-at} u(t)$; $a > 0$
- (ii) $x(t) = e^{at} u(-t)$; $a > 0$
- (iii) $x(t) = \delta(t)$
- (iv) $x(t) = A \cdot \text{Rect}(t/T)$
- (v) $x(t) = \text{sgn}(t)$

3. For $x(t)$ shown in figure:



Find:

- (i) $\int_{-\infty}^{\infty} X(\omega) d\omega$
- (ii) $X(0)$
- (iii) $\int_{-\infty}^{\infty} X(\omega) e^{j4\omega} d\omega$

4. Let $x(t)$ be a periodic signal with fundamental time period 'T' and fourier series coefficient a_k . Derive the fourier series coefficient of each of the following signals in terms of a_k .

(i) $x(t-t_0)+x(t+t_0)$

(ii) $\text{Even}\{x(t)\}$

(iii) $\text{Real}\{x(t)\}$

(iv) $x(3t-1)$

5. Find Fourier series coefficient of $x(t) = \sum_{m=-\infty}^{\infty} \delta(t - mT)$